

Free Fall

A bit of history...

Aristotle (Greek philosopher/scientist) divided motion into two main classes:

1. *Natural Motion* – results from “nature” of objects

- Clay (from the earth) will fall to the ground
- Smoke (being of air) rises
- Feather (mostly Earth, a little air) falls to the ground but not as fast as clay

*Objects fall at speeds proportional to their weights – the heavier the object, the faster it falls

2. *Violent Motion* – pushing cart, tug of war

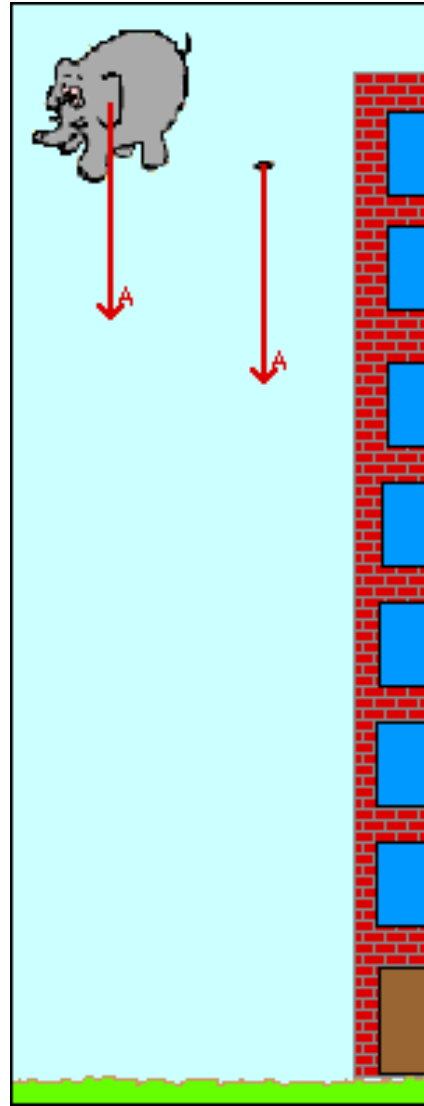
- Externally caused – outside forces cause object to move

Summary: All motions resulted from the nature of the moving object or from a sustained push or pull.

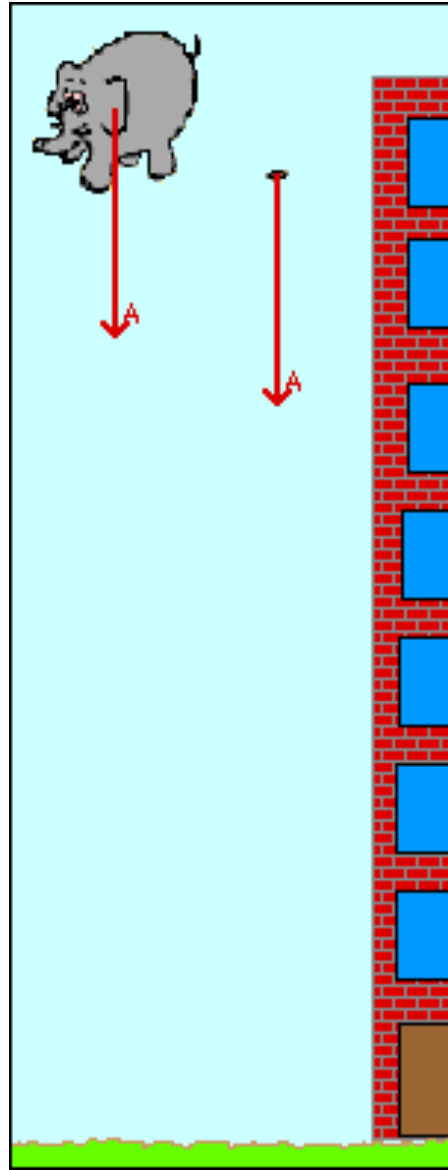
...a bit more history

- Galileo (Italy, 1600s) attempted to prove Aristotle's theories wrong.
- He drops objects of various weights from the top of the Leaning Tower of Pisa and compares the falls.
- He thinks that light objects and heavy objects will fall at the same rate.
- Galileo discovered that in the absence of air resistance all objects near the surface of earth accelerate at **-9.8 m/s²**.

The Elephant and the Feather, Free Fall



The Elephant and the Feather - Air Drag



Acceleration due to gravity, g

- If an object is in free fall, it ALWAYS accelerates at negative 'g'. ($g = 10 \text{ m/s}^2$)
- Gravity pulls objects towards earth (down), therefore we use acceleration due to gravity $a = -g$ when we are solving free fall problems
- $a = -9.8 \text{ m/s}^2$ for ANY object in free fall – ALWAYS!

One Dimensional Motion: Recipe

1. Draw a cartoon with the coordinate axis at ground level.
2. Label the diagram with the given information.
3. Pick the proper equation and solve!

- $v_{\text{top}} = 0 \text{ m/s}$
- If an object is dropped, $v_0 = 0 \text{ m/s}$
- $t_{\text{rise}} = t_{\text{fall}}$ when objects return to same height
- $a = -9.8 \text{ m/s}^2$

Formulas for Constant Acceleration

1. $v = at + v_0$

2. $s - s_0 = \bar{v}t = \left(\frac{v+v_0}{2}\right)t$

3. $s = \frac{1}{2}at^2 + v_0t + s_0$

4. $v^2 - v_0^2 = 2a(s - s_0)$

Notes:

1. If time is not involved in the problem, use equation 4.
2. If time is involved in the problem as a given value or as the unknown, use equation 1 or 3.
3. At the zenith, vertical velocity $v_y=0$.
4. For initial velocities:
 1. $V_0=0$ if we drop the ball
 2. $V_0= (+)$ if we toss it upward
 3. $V_0= (-)$ if we throw it downward

Conceptual Examples

Ex1: A ball is dropped off a cliff. What is its speed after 4 s? 9 s?

Ex2: A ball is tossed straight up at 30 m/s. How long does it take to reach max height? How long is it in the air?

Ex: A gumdrop is released from rest at the top of the Empire State Building, which is 381 m tall. Ignoring air resistance, calculate:

a) the total time the gumdrop is in the air

b) Its displacement at 3.00 s

c) Its final velocity

Example: Brad throws an orange straight up at 60 m/s.

- a) Find the total time airborne
- b) Find the time to the apex
- c) Find the location at the zenith
- d) Find the velocity with which it hits the ground
- e) Find the time at which the speed is 20 m/s