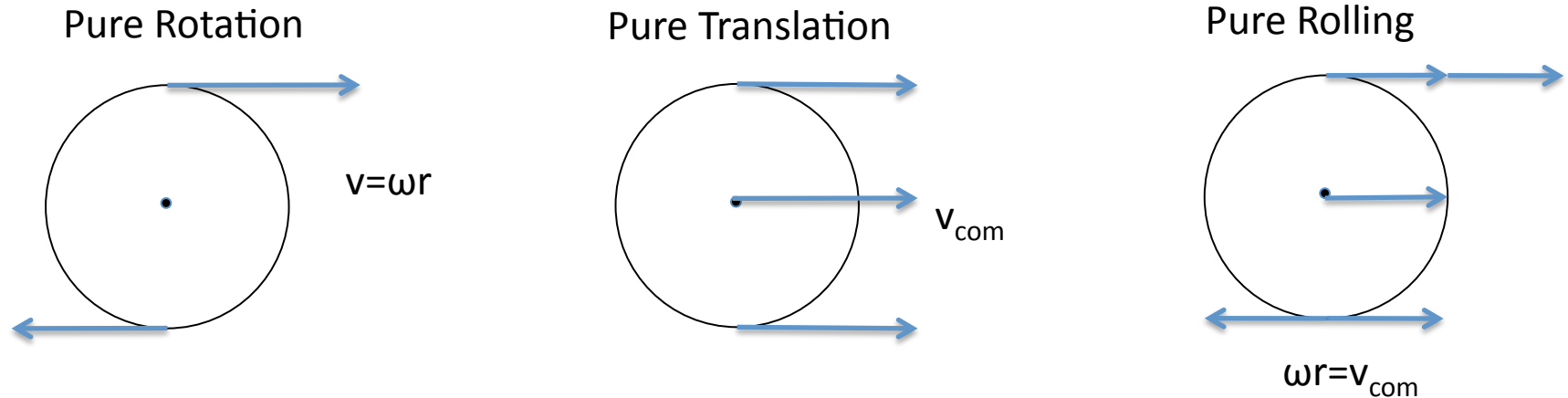


# Conservation of Energy

# Conservation of Energy

- As usual, we will set initial energy equal to final energy.
- If an object starts higher than its later position, it will have potential energy at the start.
- For falling shapes, we will note how far its **center of mass** descends.
- If an object is spinning, it will have rotational kinetic energy.
- If the axis an object is rotating around is moving linearly, it will have translational kinetic energy.

- If a wheel rolls without slipping, the bottom of the wheel is always at rest instantaneously.



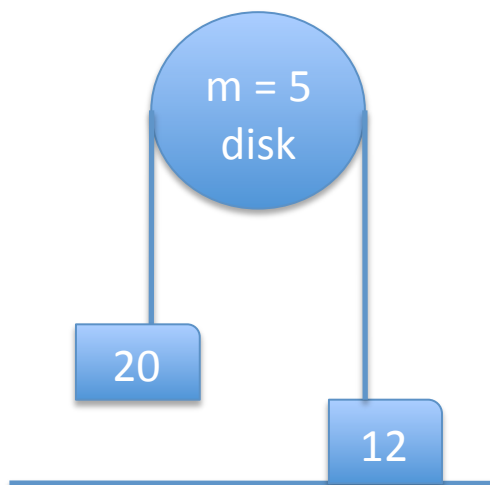
**Ex1:** A ball of mass  $M$  and radius  $R$  starts from rest at a height of 2 m and rolls without slipping down a  $30^\circ$  slope.

- A) What is the linear speed of the ball at the bottom of the hill?
- B) Would a hoop of the same mass and radius reach the same speed at the bottom of the hill?

**Ex2:** A uniform rod of length  $L$  and mass  $M$  is free to rotate on a frictionless pin passing through one end. The rod is released from rest in the horizontal position.

- A) What is the rod's angular speed when it reaches its lowest point?
- B) Determine the linear speed of the end of the rod when it is at its lowest position.

**Ex3:** What is the speed of the 12 kg block when the 20 kg block hits the ground? The system is released from rest when the 20 kg block is 4 m off the ground.



## Calculating Work & Power

Linear	Rotational
$W = \int F dx$	$W = \int \tau d\theta$
$W = Fd \cos \theta$	$W = \tau \theta$
$W_{net} = \Delta K$	$W = \Delta \frac{1}{2} I \omega^2$
$\bar{P} = \frac{W}{t}$	<i>same</i>
$P = Fv$	$P = \tau \omega$